

Controle de Sistemas Dinâmicos

CSD – Exercícios Cap9 Projetos de Controle no LGR

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(Material de aula *Complementar*)

o projeto do controlador

é feito em função do **polo dominante**

-> todas as restrições devem ser atendidas assumindo-se um sistema “ideal” de 2ª ordem sem zeros.

O projeto de sistemas “reais” não será “**exato**”.

Algumas especificações

- não completamente atendidas,
- outras sobre-atendidas!!

```
zeta = -log(Mp/100)/sqrt(pi*pi+log(Mp/100)^2)
sigma=4/ts
wn=1.8/tr
wd=pi/tp

i=pi/2+.01:0.01:pi-.01; x=wn*cos(i);y=wn*sin(i);
plot(x,y,'k--','LineWidth',2);hold on;
plot([-sigma -sigma],[0 maxGr]*1,'r--','LineWidth',2);
plot([-maxGr 0],[wd wd],'g--','LineWidth',2);
plot([-maxGr 0]*1,[maxGr/tan(asin(zeta)) 0]*1,'b--','LineWidth',3)

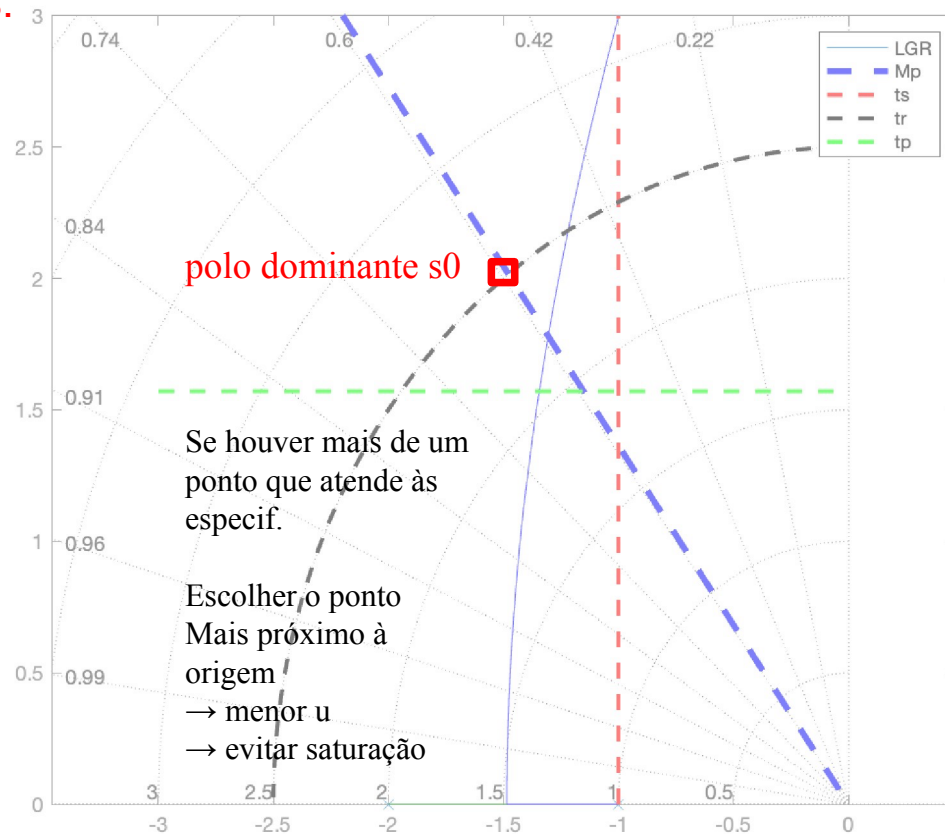
title('Especificação no plano s = $\sigma + $j$\omega$', ...
      'fontsize',16,'interpreter','latex')
ylabel(''),xlabel('')

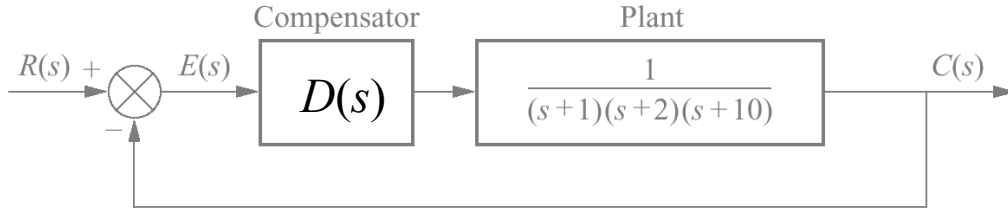
axis([-maxGr 0 0 maxGr]); axis equal;
legend('LGR','tr','ts','tr','Mp')
```

especific_t2s(G,maxGr,Mp,ts,tr,tp) → .../CSD.html

g=zpk([],[-1 -2 -10],1)

especific_t2s(g,3,10,4,1.8/2.5,2)





- $e_{ss} \leq 0.01$
- $t_s \leq 6 \text{ s}$
- $M_p \leq 40\%$
- $t_r \leq 1.8 \text{ s}$

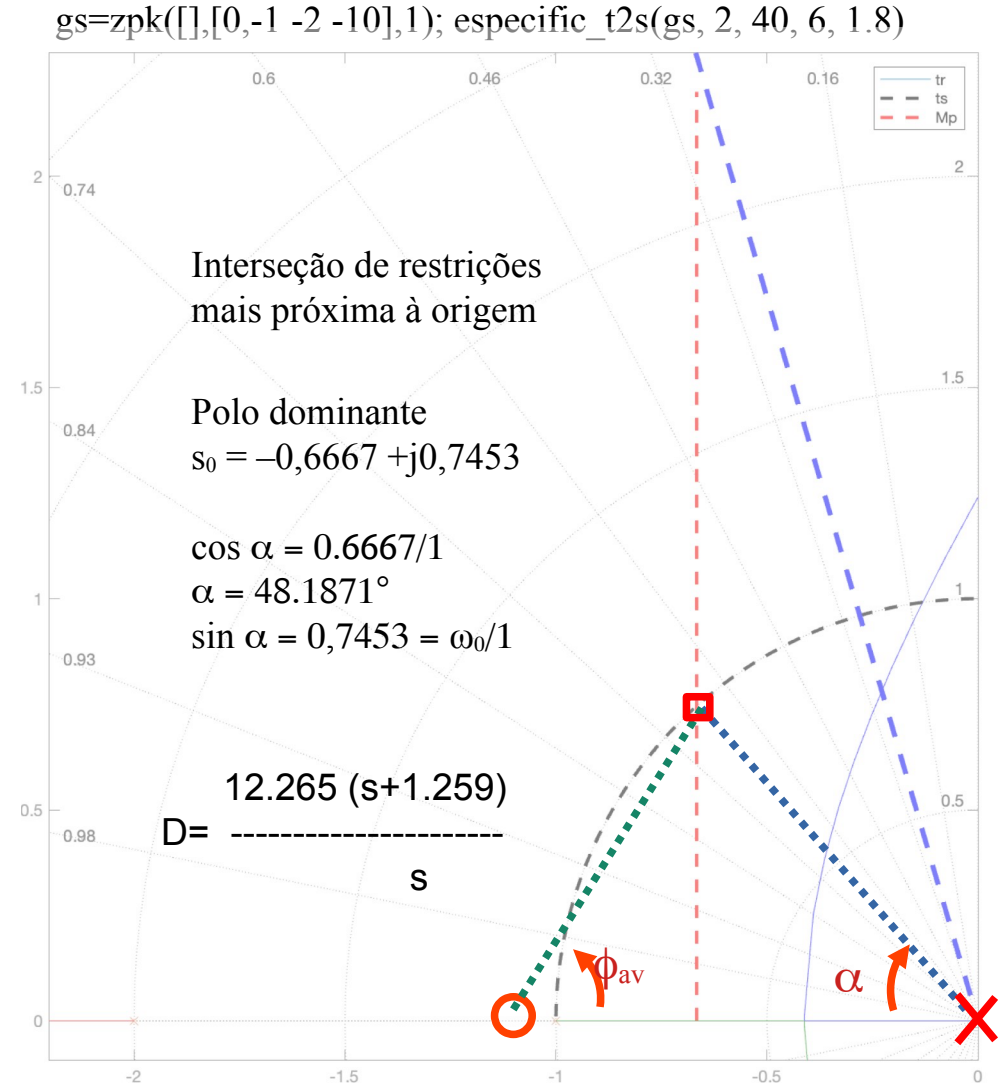
```
s=-.667+j*.7453; 180-angle(1/(s*(s+1)*(s+2)*(s+10)))*180/pi
```

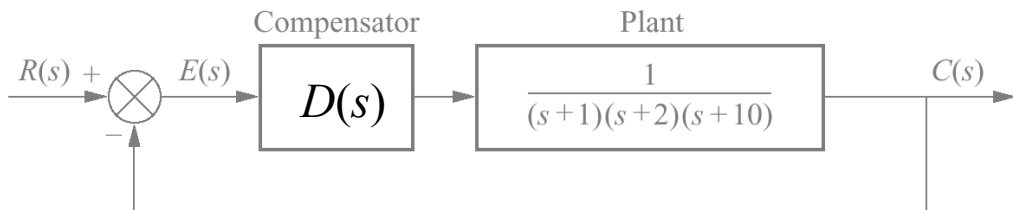
$$\phi_{av} = 51.52^\circ$$

$$\tan \phi_{av} = .7453/\Delta \rightarrow \Delta=0.5924 \Rightarrow z = -1.259$$

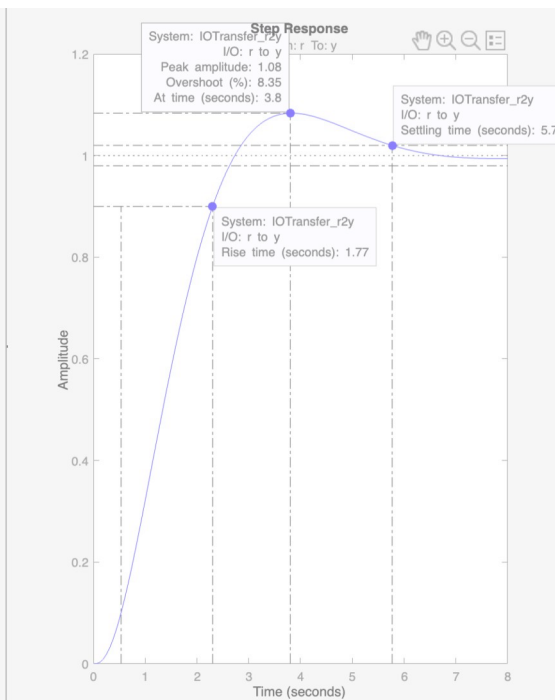
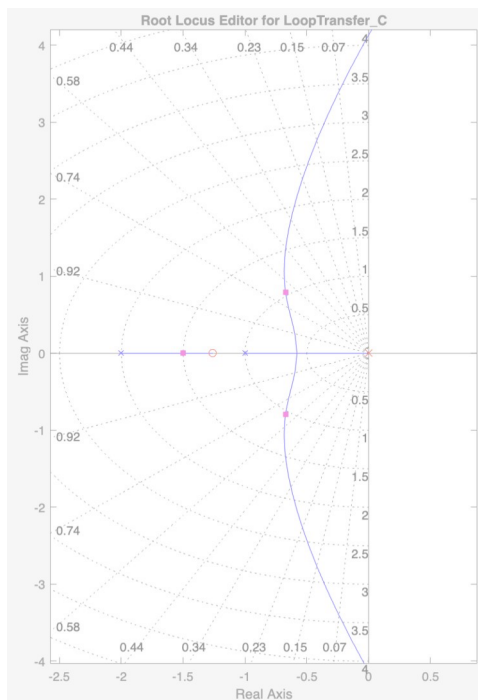
```
s=-.667+j*.7453; abs((s*(s+1)*(s+2)*(s+10))/(s+1.259))
```

$$K = 12.2655$$





$M_p \rightarrow$ sobre-atendido!



Especificações: $\text{especific_t2s}(\text{gs}, 40, 6, 1.8)$

- $e_{ss} \leq 0.01$
- $t_s \leq 6$ s
- $M_p \leq 40\%$
- $t_r \leq 1.8$ s

Interseção de restrições
mais próxima à origem

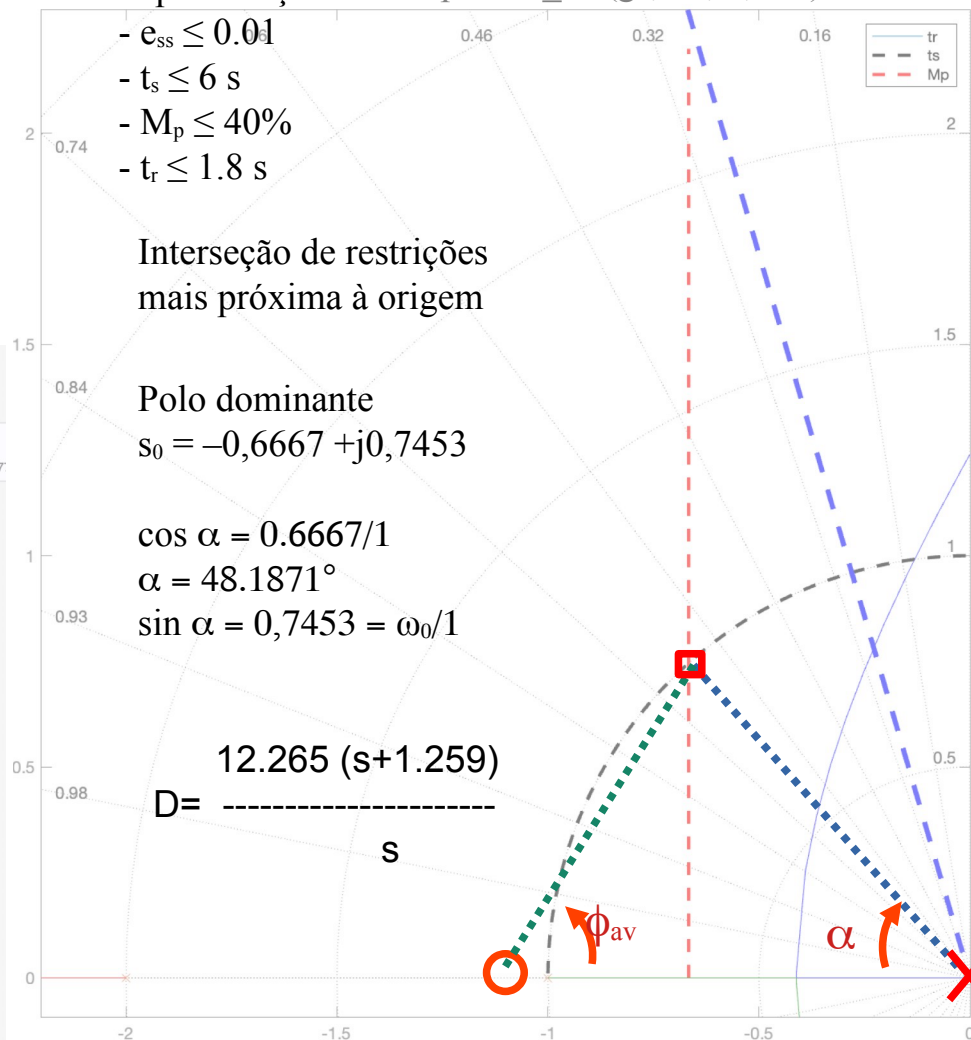
Polo dominante
 $s_0 = -0,6667 + j0,7453$

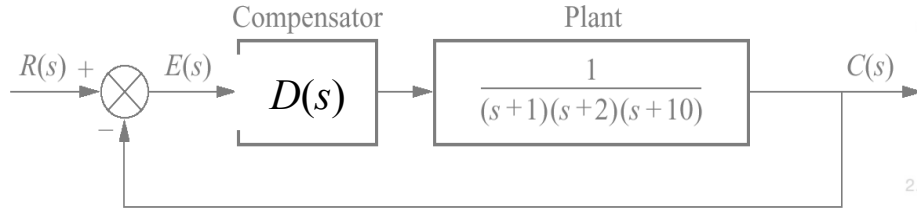
$$\cos \alpha = 0.6667/1$$

$$\alpha = 48.1871^\circ$$

$$\sin \alpha = 0,7453 = \omega_0/1$$

$$D = \frac{12.265 (s+1.259)}{s}$$





Especificações:

- $e_{ss} \leq 0.01$
- $t_s \leq 4$ s
- $M_p \leq 10\%$
- $t_r \leq 1.8/2.5$ s

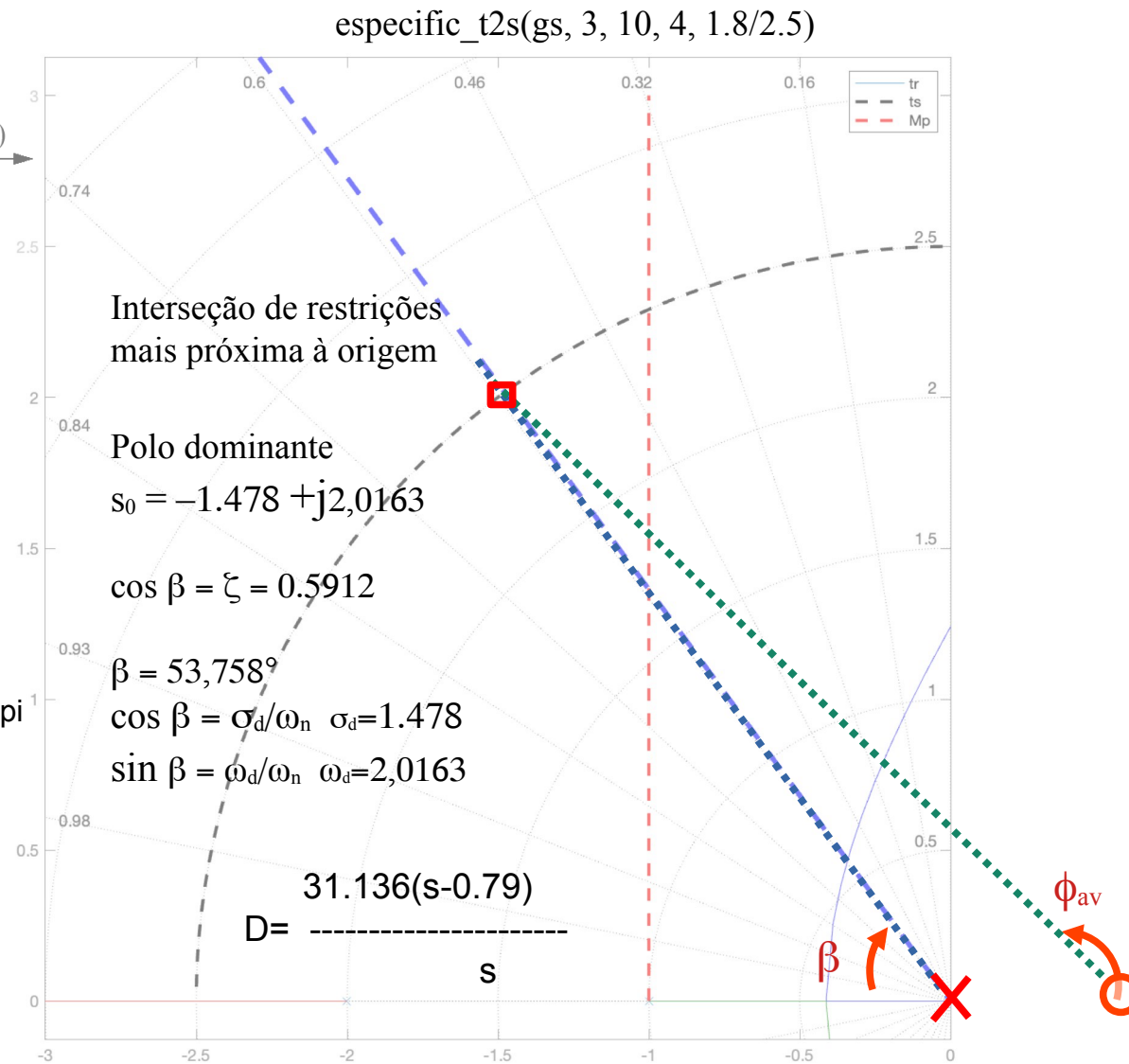
Canal I: $\phi_{av} = 180^\circ - \angle G(s)/s$ s_0

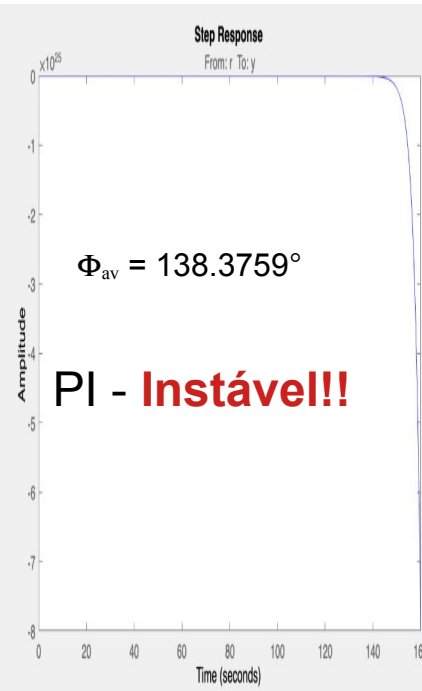
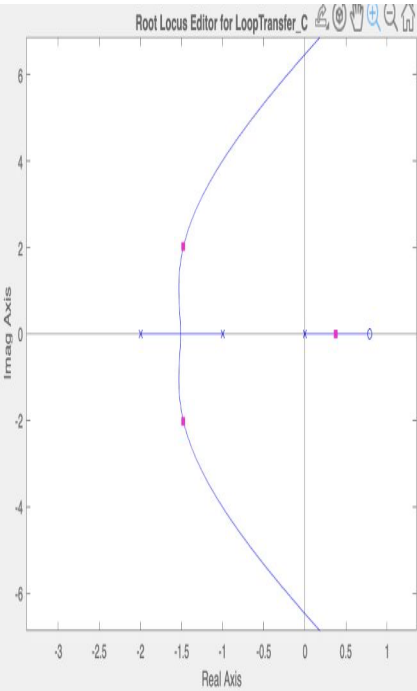
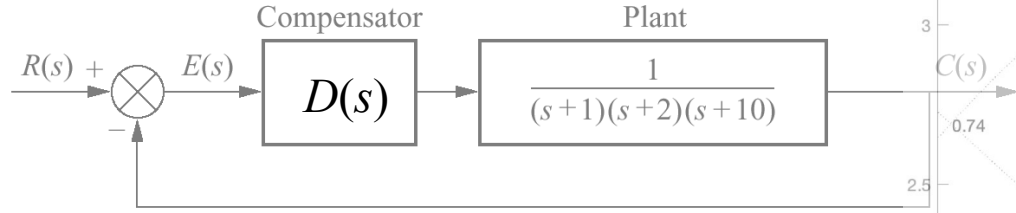
$s = -1.478 + j2.0163$; $180 - \angle(1/(s*(s+1)*(s+2)*(s+10))) * 180/\pi$
 $\Phi_{av} = 138.3759^\circ$

$\tan(180^\circ - \phi_{av}) = 2.0163/\Delta \rightarrow \Delta = 2.2691 \Rightarrow z = -1.478 + 2.2691$
 $z = 0.79$ (Semi-plano direito. Fase não-mínima!!)

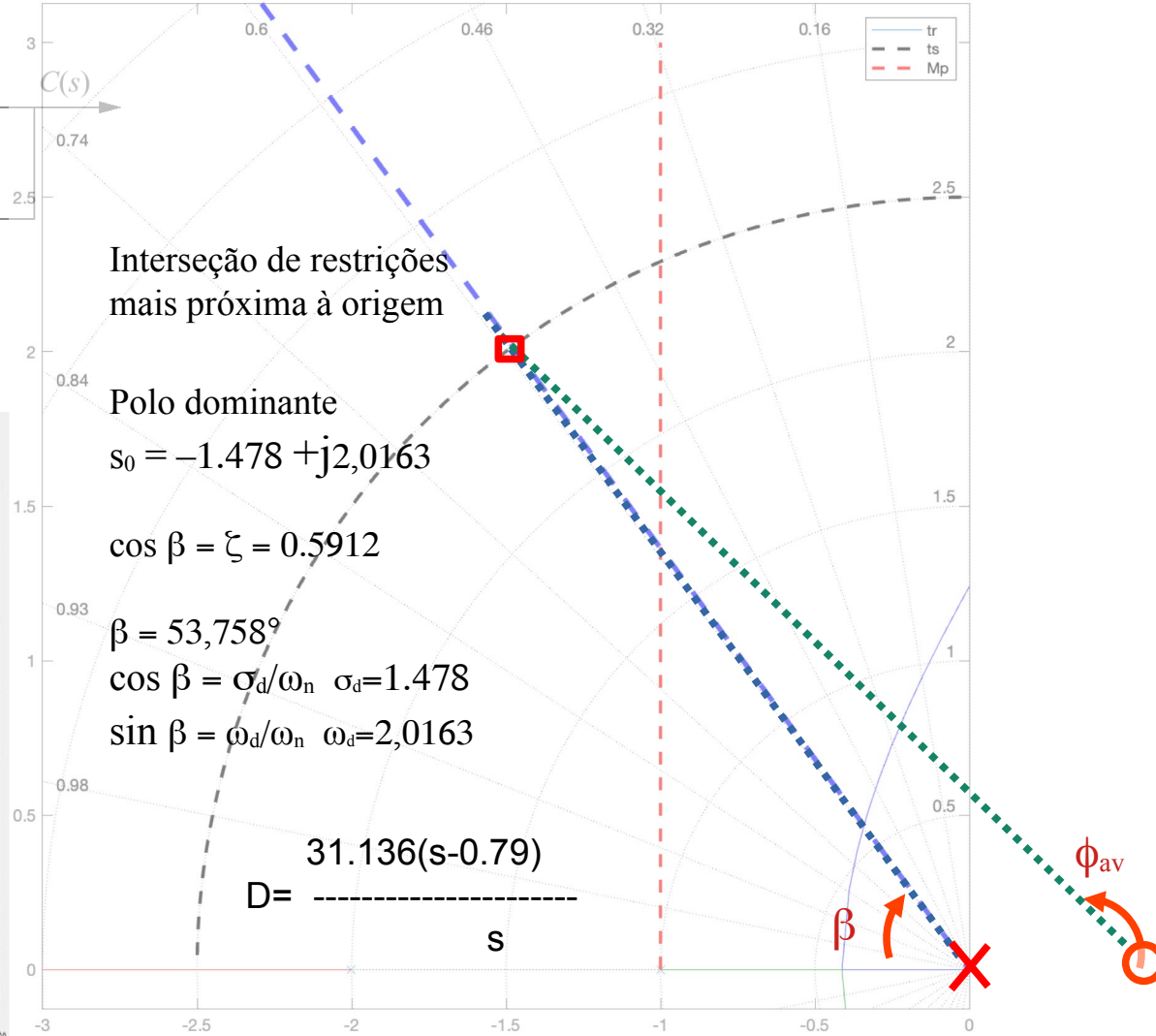
Condição $|| \rightarrow K|DG| = 1$

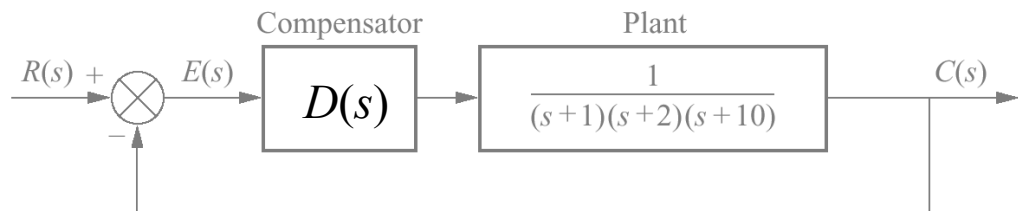
$s = -1.478 + j2.0163$; $\text{abs}((s*(s+1)*(s+2)*(s+10))/(s-0.79))$
 $K = 31.1362$





especific_t2s(gs, 3, 10, 4, 1.8/2.5)





PID com zero duplo: $\Phi_{av}/2 = 69.188^\circ$

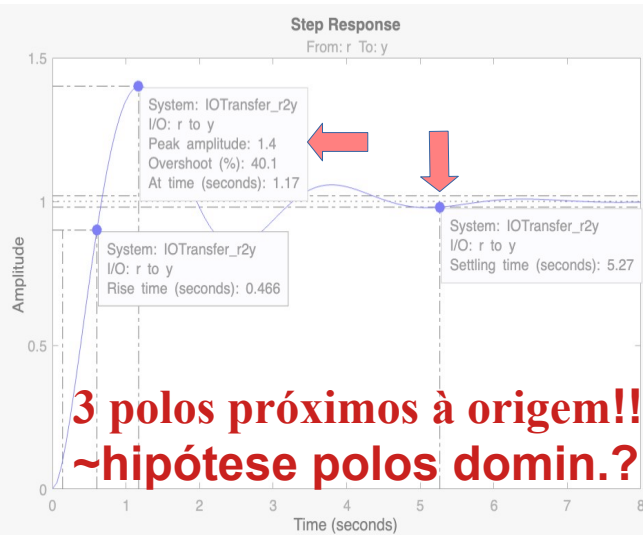
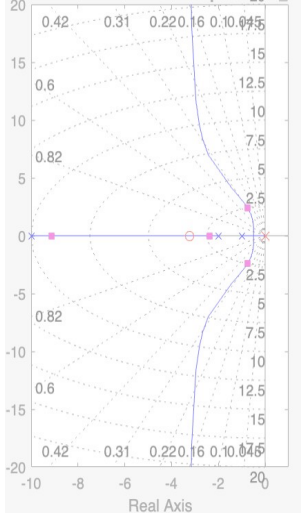
$\tan(180^\circ - \Phi_{av}/2) = 2.0163/\Delta \rightarrow \Delta = 1.7489 \Rightarrow z = -3.2269$

Condição $|| \rightarrow K|DG| = 1$

$s = -1.478 + j2.0163$; $\text{abs}((s*(s+1)*(s+2)*(s+10))/(s+3.2269)^2)$

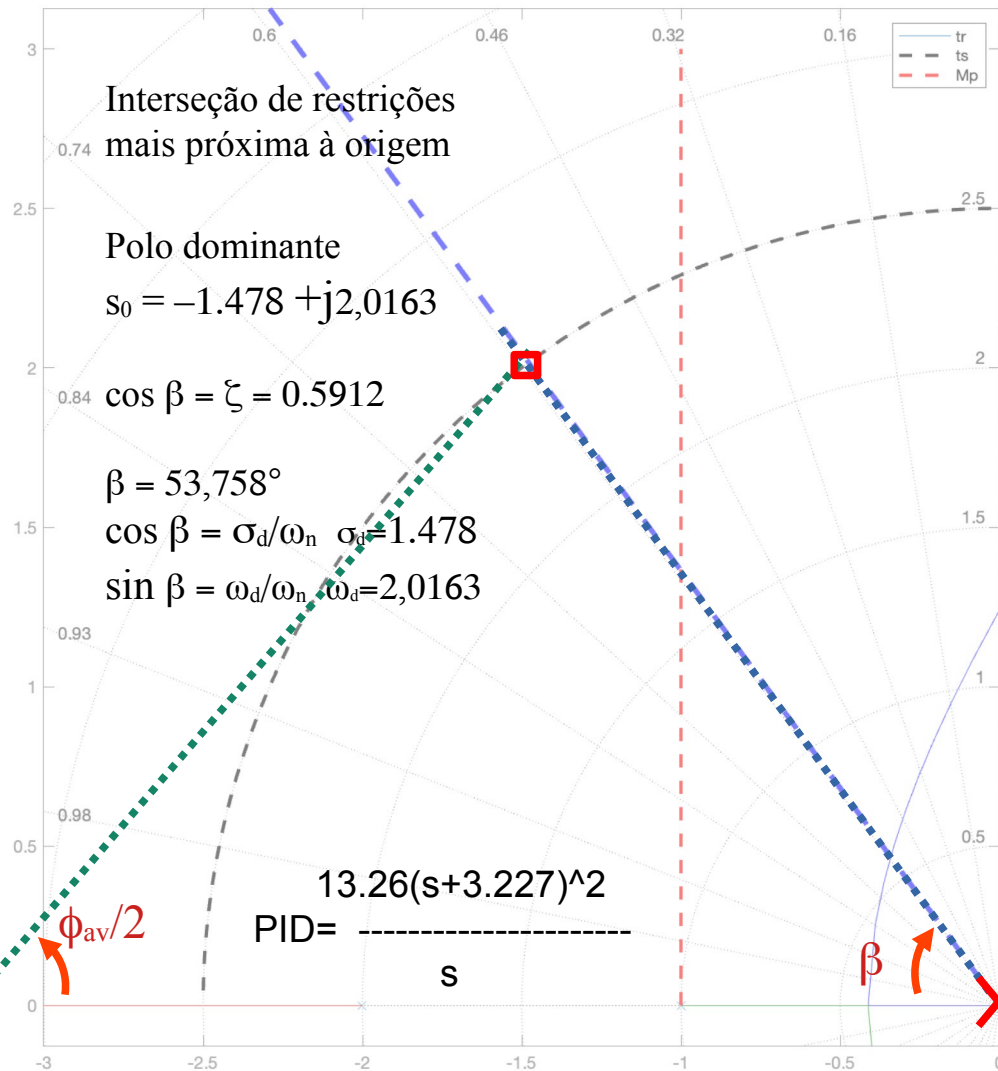
$K = 13.2632$

Root Locus Editor for LoopTransfer_C



**3 polos próximos à origem!!
~hipótese polos domin.?**

especific_t2s(gs, 3, 10, 4, 1.8/2.5)



PID cancelando polo em -2 (LGR leva polos em 0 e -1 p/ esquerda).

$$\phi_{av2} = 180^\circ - \angle \frac{(s+2)G(s)}{s} \Big|_{s_0}$$

$$s = -1.478 + j*2.0163; 180 - \angle(1/(s*(s+1)*(s+10))) * 180/\pi$$

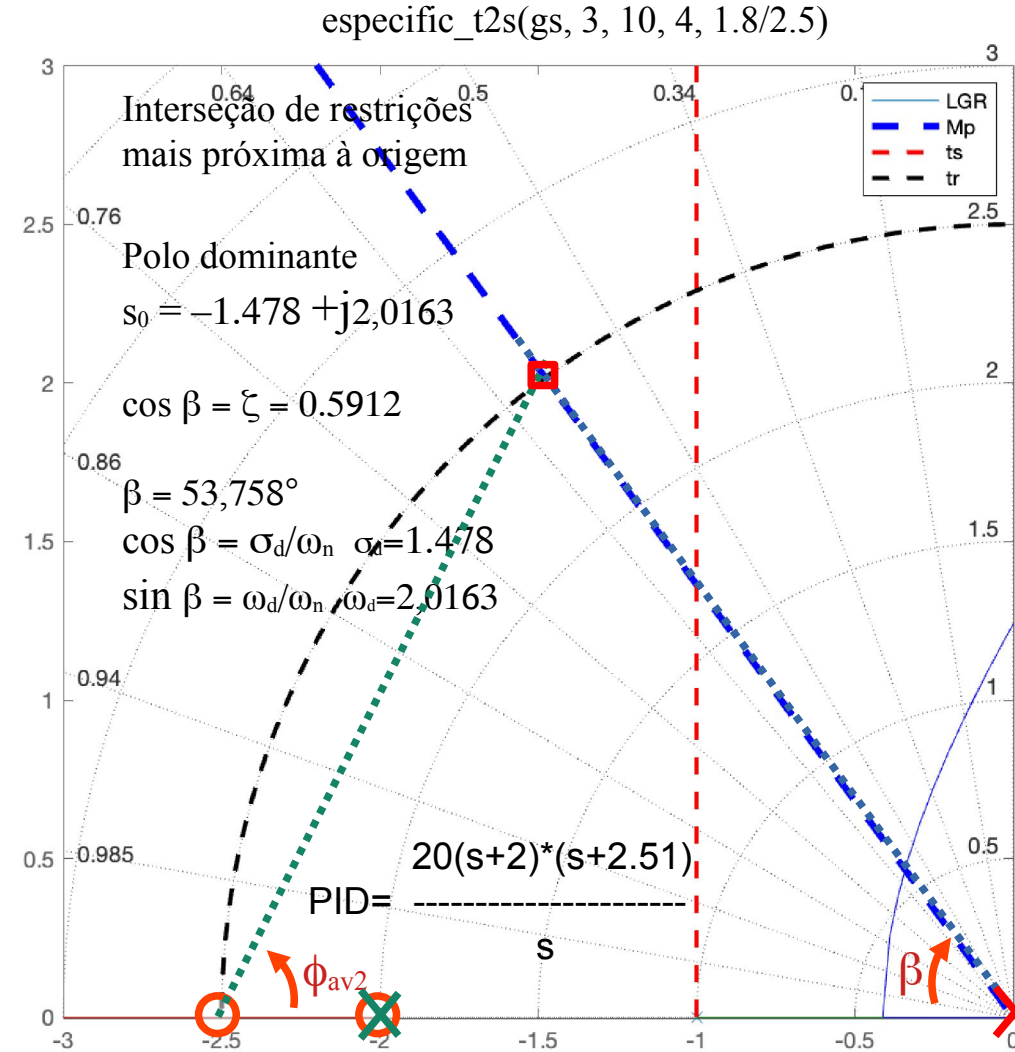
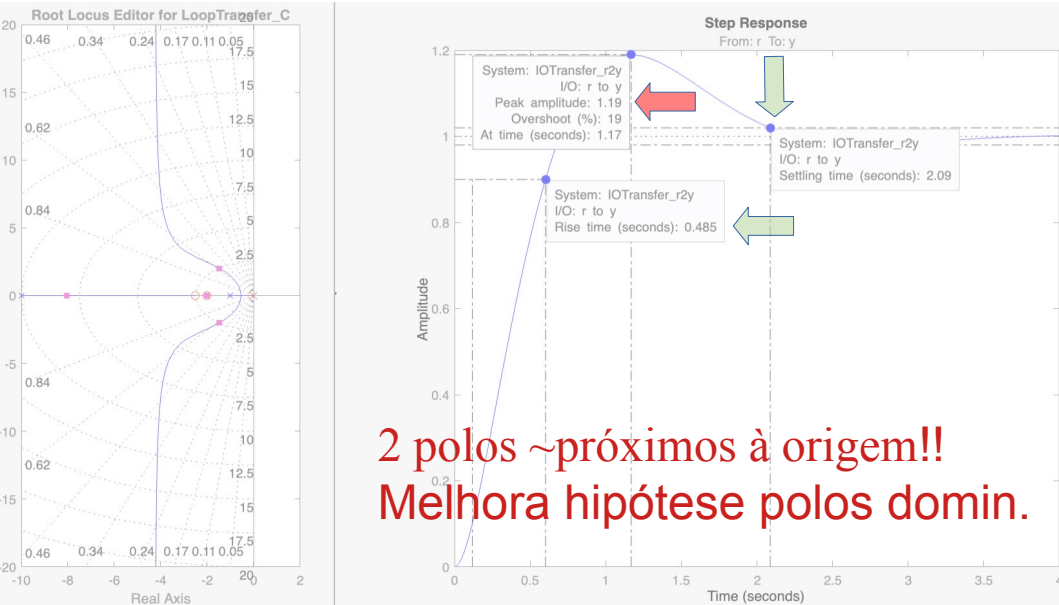
$$\Phi_{av2} = 62.89^\circ$$

$$\tan(\phi_{av2}) = 2.0163/\Delta \rightarrow \Delta = 1.0322 \Rightarrow z = -2.51$$

Condição $|| \rightarrow K|DG| = 1$

$$s = -1.478 + j*2.0163; \text{abs}((s*(s+1)*(s+10))/(s+2.51))$$

$$K = 20$$



Compensador em Avanço: $\phi_{av} = 180^\circ - \angle G(s)_{s_0}$

$s = -1.478 + j*2.0163$; $180 - \angle(1/((s+1)*(s+2)*(s+10))) * 180/\pi$

1. Compensador em Avanço: $\Phi_{av} = 12.1335^\circ$

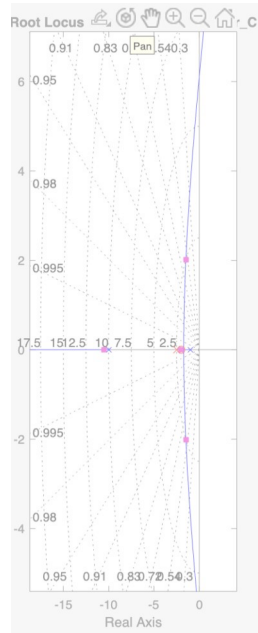
$s = -1.478 + j*2.0163$, $\angle(s+2) - \angle(s+z) = 12.1335^\circ$

$\angle(s+z) = \angle(s+2) - 12.1335^\circ = 75.485 - 12.133 = 63.352^\circ$

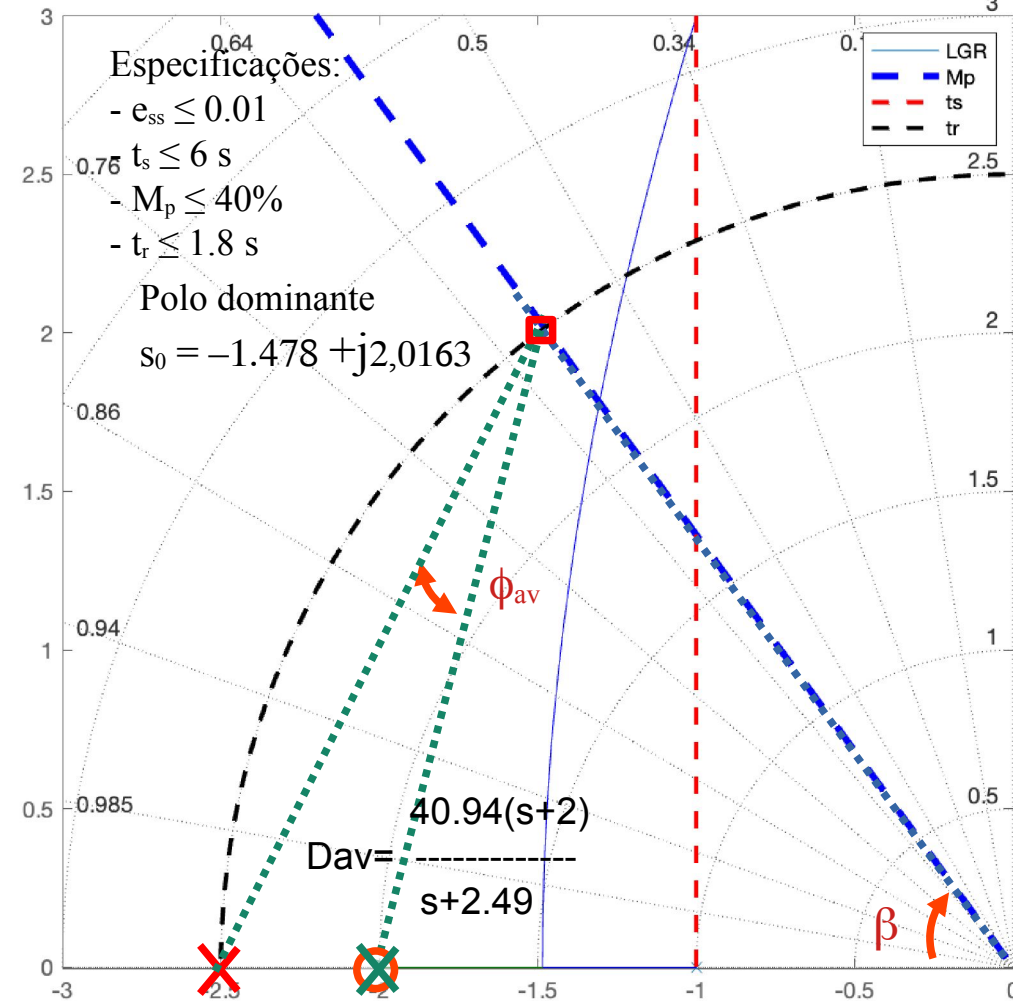
$\tan(\phi_{av}) = 2.0163/\Delta \rightarrow \Delta = 1.0118 \Rightarrow p = -2.4898$

Condição $|| \rightarrow K|DG| = 1$

$s = -1.478 + j*2.0163$; $\text{abs}(((s+1)*(s+10)*(s+2.49)))$, $K = 40.94$



$g = \text{zpk}([], [-1 -2 -10], 1)$; $\text{especific_t2s}(g, 3, 10, 4, 1.8/2.5)$



Compensador em Avanço: *Método da Bissetriz*

$$s = -1.478 + j*2.0163; 180 - \angle(1/((s+1)*(s+2)*(s+10))) * 180/\pi$$

$$\Phi_{av} = 12.1335^\circ$$

$$s = -1.478 + j*2.0163, \angle(s+2) - \angle(s+z) = 12.1335^\circ$$

$$71.88 \pm 12.1335^\circ = 77.9458^\circ / 65.8123^\circ$$

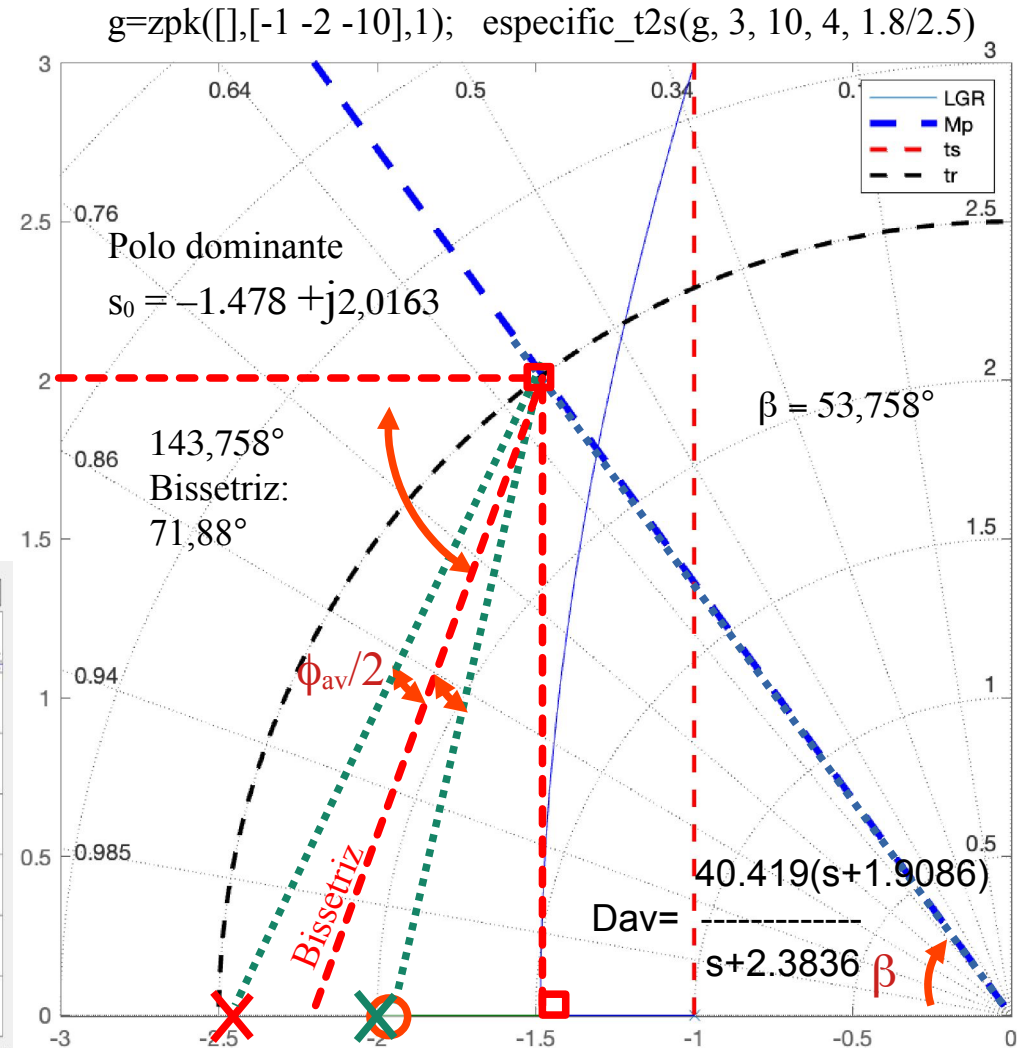
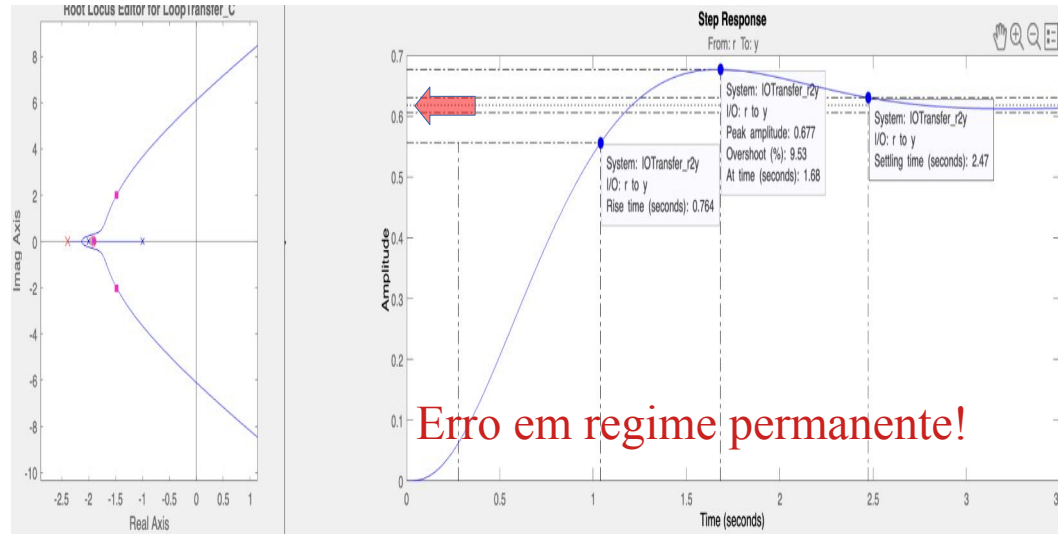
$$\text{Tand}(90 - 77.9458) * 2.0163 + 1.478 = 1.9086 = z$$

$$\text{Tand}(90 - 65.8123) * 2.0163 + 1.478 = 2.3836 = p$$

$$\text{Condição } || \rightarrow K|DG| = 1$$

$$s = -1.478 + j*2.0163;$$

$$\text{abs}(((s+1)*(s+2)*(s+10)*(s+2.3836)/((s+1.9086))), K = 40.419$$



2. Compensador em Avanço-Atraso: (acrescentando atraso).

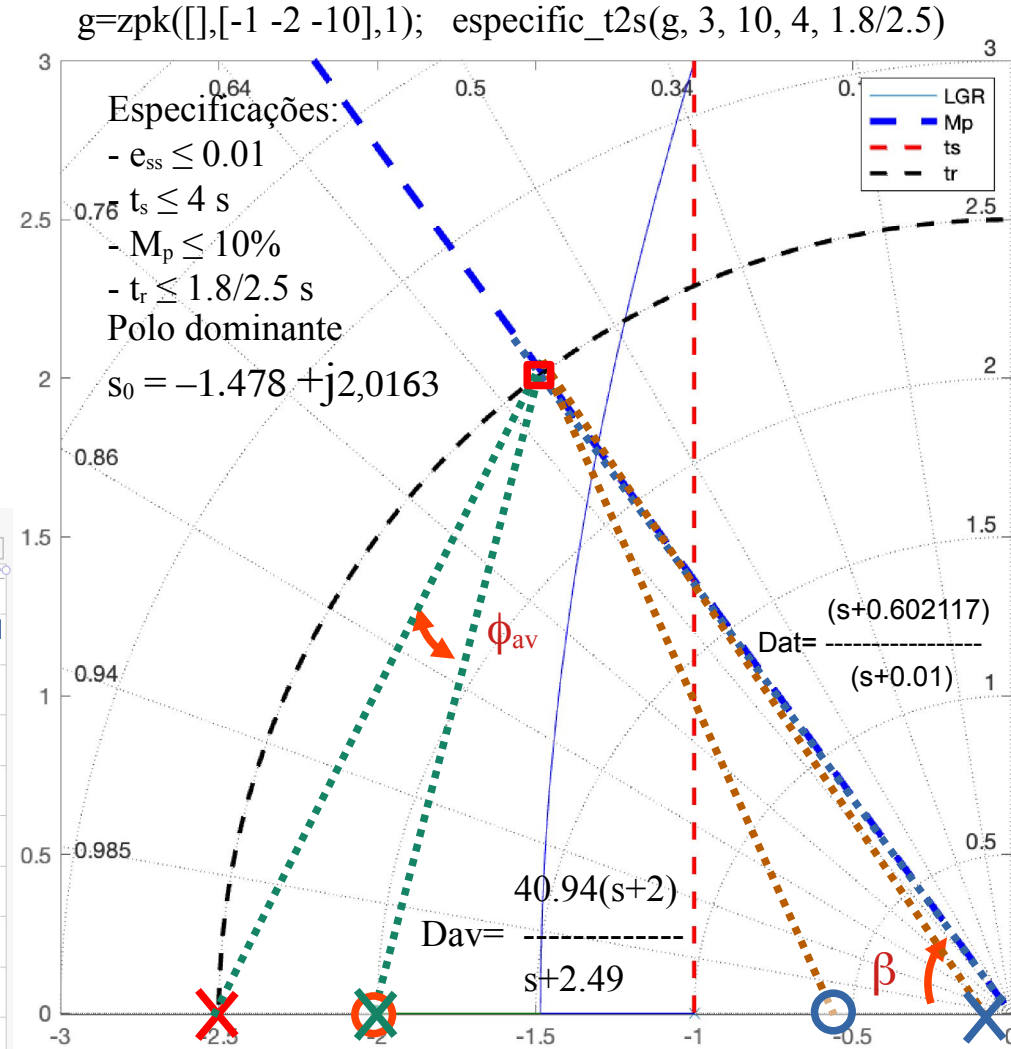
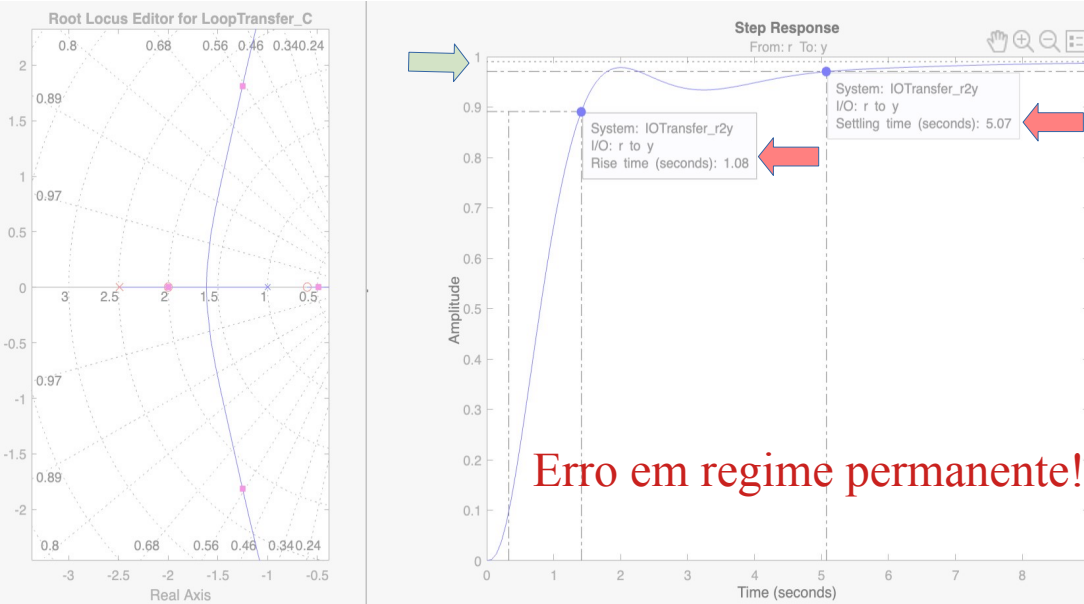
Condição $|| \rightarrow K|DG| = 1$

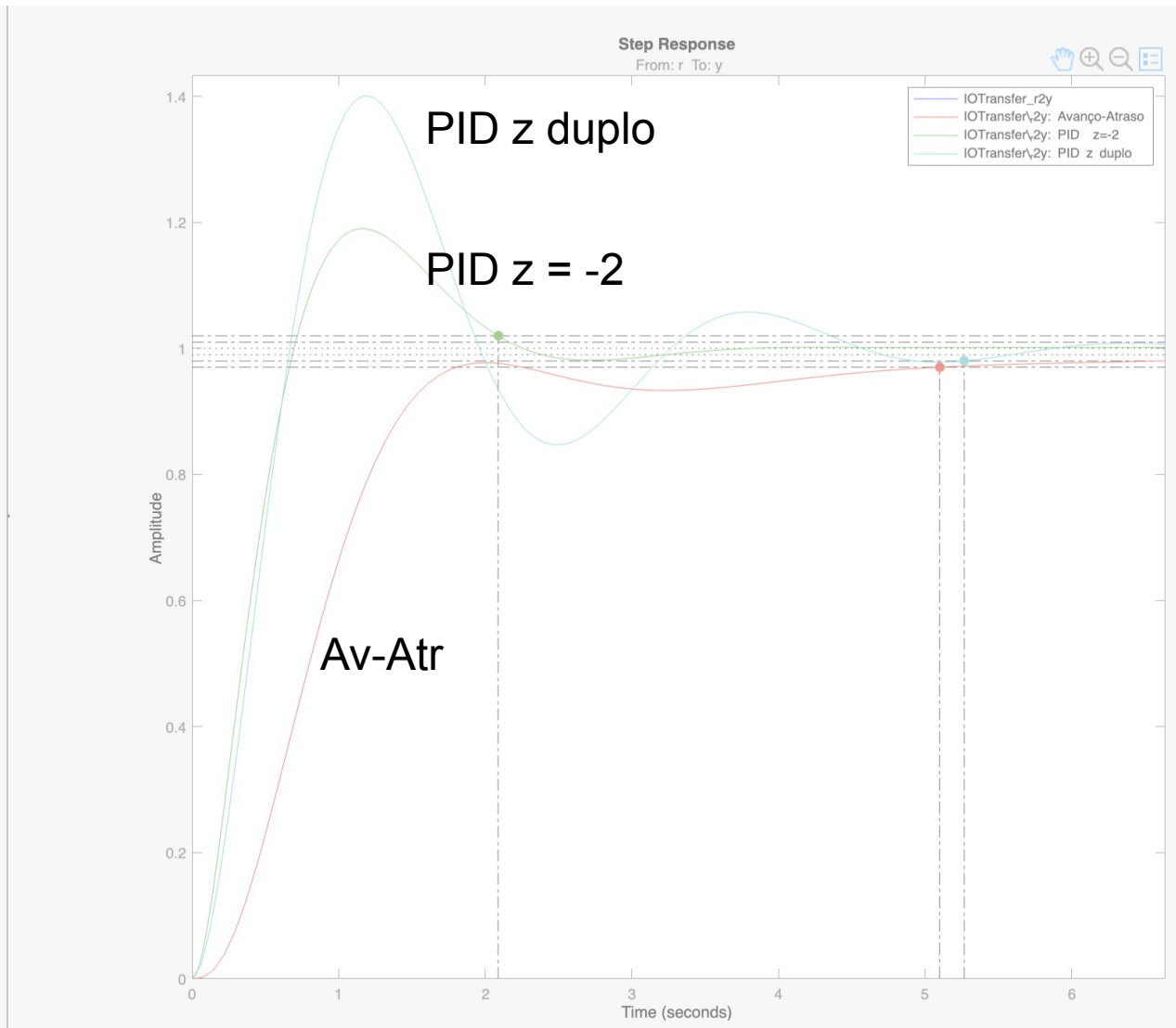
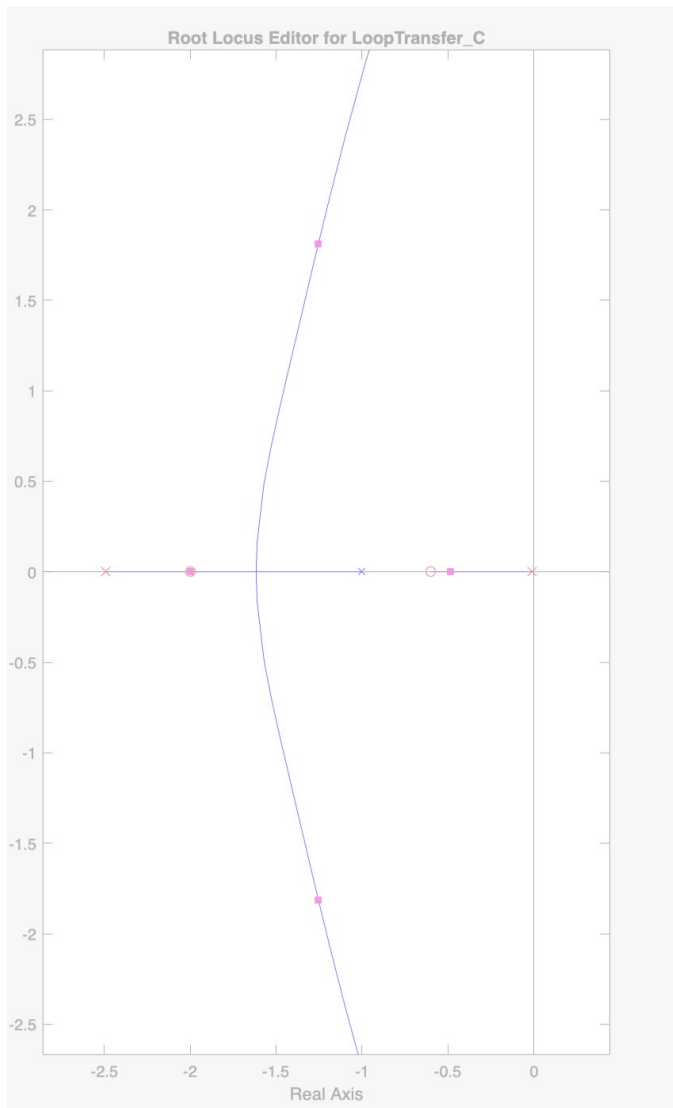
$s = -1.478 + j2.0163$;

$40.94/((s+1)*(s+10)*(s+2.49))$, $K_p = \lim_{s \rightarrow 0} s \cdot 1/s () = 1.6442 \Rightarrow e_{ss} = 0,3782$

$1/(1+Kp') = 0.01 \rightarrow Kp' = 99 \quad Kat = 99/1.6442 = 60.2117$

$\rightarrow Dat = (s+0.602117)/(s+0.01)$





2. Compensador em Avanço-Atraso: (cancelando polo em -1).

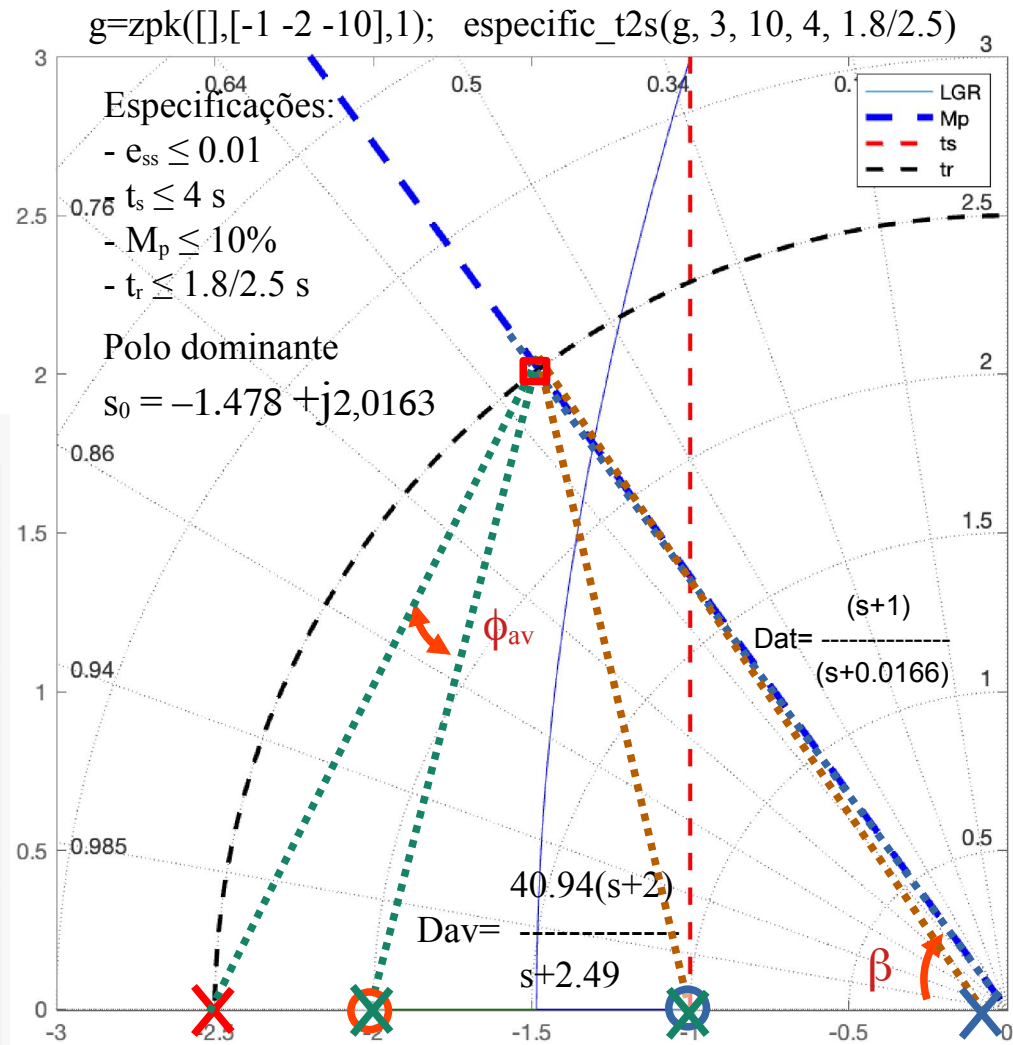
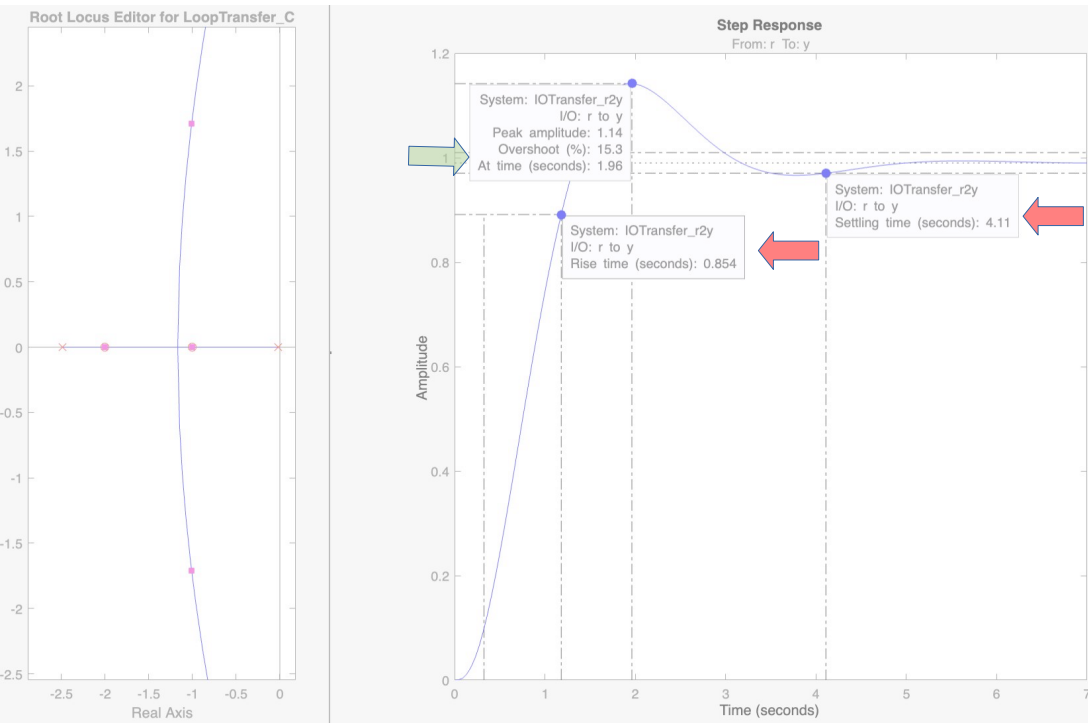
Condição $| | \rightarrow K|DG| = 1$

$s = -1.478 + j2.0163$;

$40.94/((s+1)*(s+10)*(s+2.49))$, $K_p = \lim_{s \rightarrow 0} s \cdot 1/s = 1.6442 \Rightarrow e_{ss} = 0,3782$

$1/(1+K_p') = 0.01 \rightarrow K_p' = 99 \quad K_{at} = 99/1.6442 = 60.2117$

$\rightarrow Dat = (s+1)/(s+0.0166)$



Especificações: $e_{ss}=0.01$, $M_p=10\%$, $t_s=4s$, $t_r=0.72$

PID: $e_{ss}=0.0$, $M_p=19\%$, $t_s=2s$, $t_r=0.485$

Av-Atr: $e_{ss}=0.01$, $M_p=15,3\%$, $t_s=4,11s$, $t_r=0.854$

